

SHIFT SCHEDULING FOR TRAIN DISPATCHERS



Rabii Zahir

PhD student, LiU





PROJECT FINANCED BY TRAFIKVERKET:
**CAPACITY MODELING AND SHIFT
OPTIMIZATION FOR TRAIN DISPATCHERS**
CAPMO-TRAIN



TOMAS LIDÉN, LIU

CHRISTIANE SCHMIDT, LIU

RABII ZAHIR, LIU

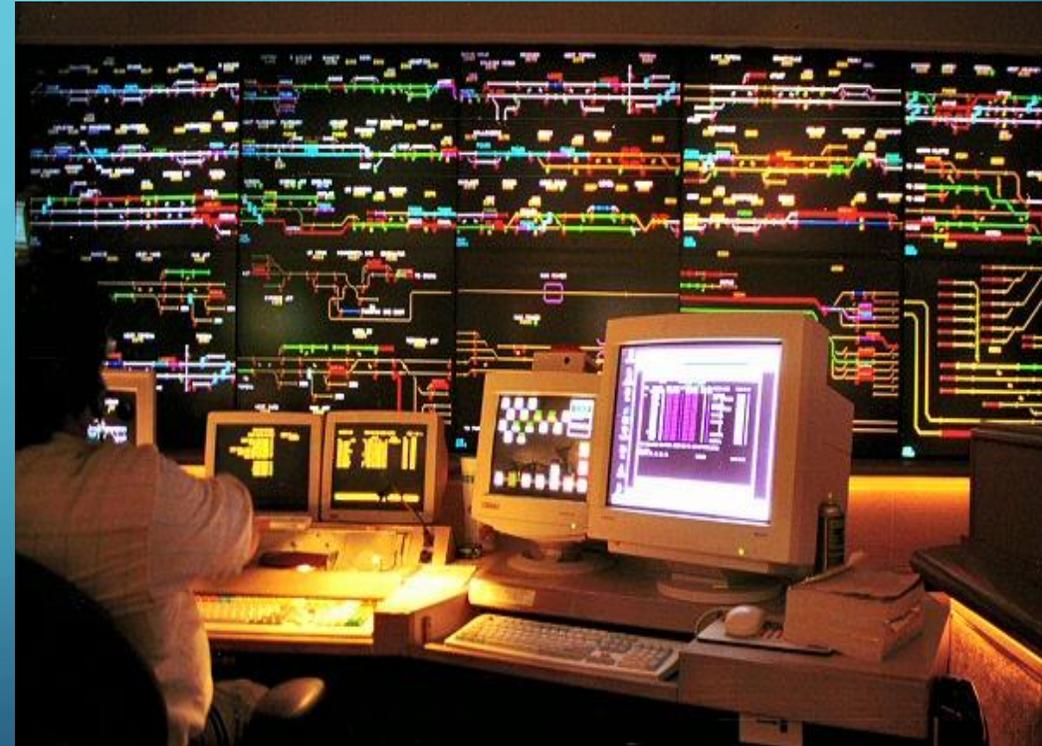


Jan Andersson, VTI

Gunilla Björklund, VTI

TRAIN DISPATCHING

- Monitoring & controlling train traffic
- Routing trains
- Open/close railway bridges
- Issue forms, truck warrants, truck permits
- Grant permission to pass red signals
- Communicate by radio/phone with train drivers and other personal
- And more...



Source for the image:

<http://www.diplomacyandcommerce.rs/serbian-trains-will-be-even-safer-and-faster-thanks-to-russian-technology/>

PROBLEM DESCRIPTION: SHIFT SCHEDULING FOR TRAIN DISPATCHERS

- Shift scheduling nowadays: manually performed
- Challenges during scheduling:
 - Legal restrictions
 - Operational restrictions
 - Balanced workload

LEGAL AND OPERATIONAL RESTRICTIONS

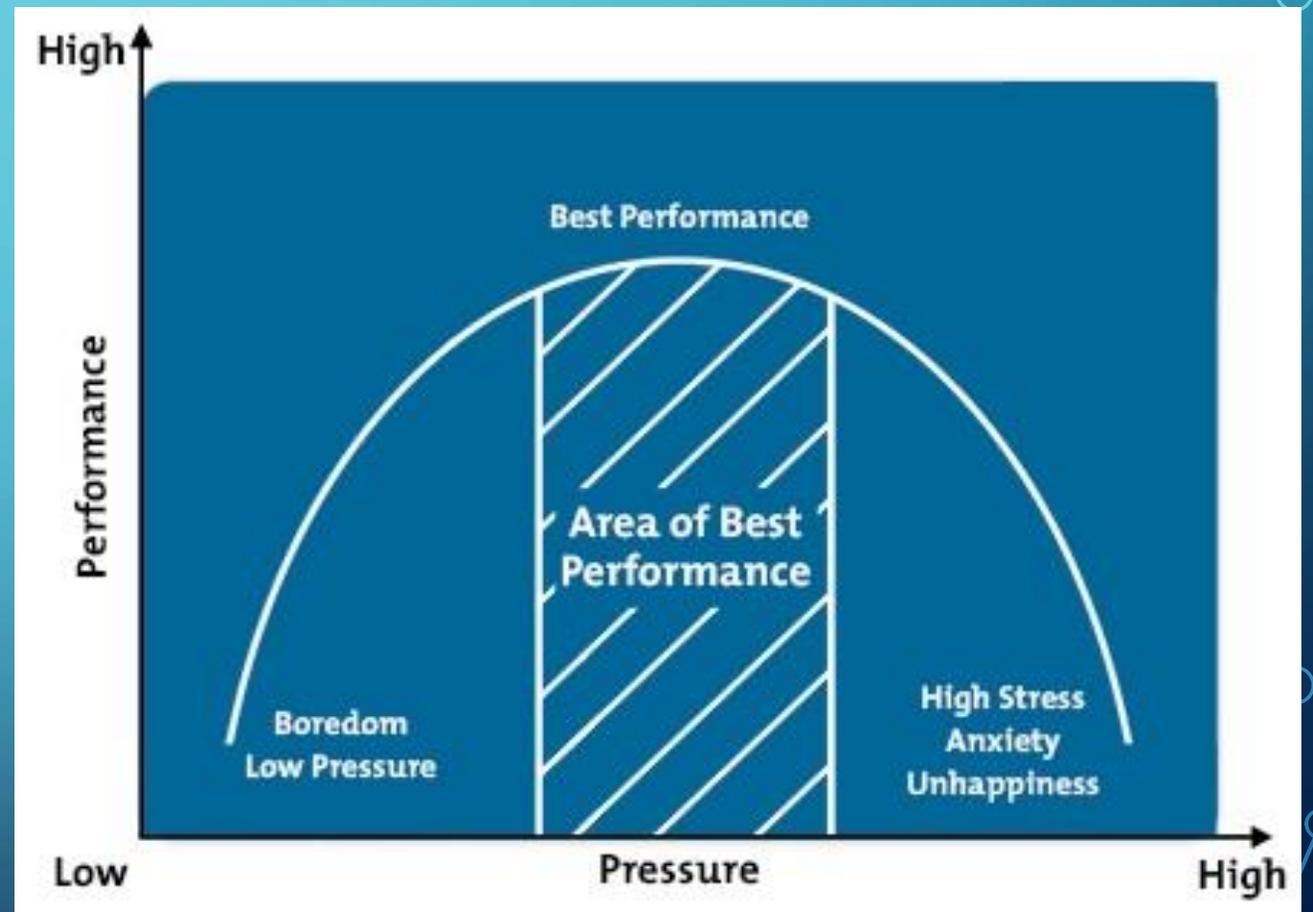


LEGAL AND OPERATIONAL RESTRICTIONS

- The min/max:
 - length of a shift; number of working hours in a time horizon (weekly); number of working days; number of working weekends; number of consecutive night shifts; number of days off after a series of night shifts
- The minimum unit that a train dispatcher can be assigned. How these units could be combined?
- How many can a dispatcher handle of: number of trains and geographical areas...?
- And more...

WORKLOAD & SAFETY

- Safety comes always first
- High workload level
- Low workload level
- Balanced workload
- Previous project (FelOP), and its extension (BelOp) run by VTI



Source: <http://www.gatewaynmra.org/2000/union-pacific-omaha-harriman-dispatch-center/>

OBJECTIVES OF THE PROJECT

The overall goal of this project is to enable Trafikverket to automatically find cost-effective and safe train dispatcher shifts:

Cost-effectiveness: minimize the number of used dispatchers (and other objectives)

Safety: workload within acceptable thresholds

In a later phase: study the effect of stochastically varying events and how to integrate it in the framework

THE OPTIMIZATION MODEL

- We used an adjusted MIP from Hernandez-Romero* et al.:
- Sets:
 - D: set of dispatchers i
 - S: set of geographic areas j
 - P: set of number of periods k

*E. Hernández-Romero, B. Joseffson, A. Lametti, T. Polishchuk, C. Schmidt, Integrating Weather Impact in Air Traffic Controller Shift Scheduling in Remote and Conventional Towers. EURO Journal on Transportation and Logistics 11 (2022)

• Parameters:

- $TL_{j,k}$: task load for each geographic area j in time period k
- TUB : upper bound on the length of dispatcher shift in interval units
- TLB : lower bound on the length of dispatcher shift in interval units
- $l_{i,j} = 1$ if dispatcher i holds endorsement to control geographic area j
- A_{max} : maximum number of areas per dispatcher
- TL_{max} : maximum task load per dispatcher
- R_{min} : minimum number of rest periods between the shifts
- R_{max} : maximum number of rest periods between the shifts
- $p = |P|$ number of periods

- Decision variables (all binaries):

- $q_i = 1$ if dispatcher i is used during some period
- $v_{i,k} = 1$ if dispatcher i starts his shift at period k
- $y_{j,k} = 1$ if dispatcher i is at work during period k
- $x_{i,j,k} = 1$ if dispatcher i is assigned to area j during period k

- **Constraints:**

- $\sum_{j \in S} x_{i,j,k} * TL_{j,k} \leq TL_{max} \quad \forall i \in D, \forall k \in P$ (max task load per dispatcher & period)
- $\sum_{j \in S} x_{i,j,k} \leq y_{i,k} * A_{max} \quad \forall i \in D, \forall k \in P$ (max number of areas per dispatcher)
- $x_{i,j,k} \leq L_{i,j} \quad \forall i \in D, \forall j \in S, \forall k \in P$ (endorsement requirement)
- $v_{i,k} \leq y_{i,k} \quad \forall i \in D, \forall j \in S, \forall k \in P$ (connect the variables)
- $y_{i,k} \geq x_{i,j,k} \quad \forall i \in D, \forall j \in S, \forall k \in P$ (connect the variables)

- **Constraints:**

- $\sum_{\mu=k+1-TLB}^k v_{i,\mu(mod p)} \leq y_{i,k} \quad \forall i \in D, \forall k \in P$ (lower bound for shift length)

- $\sum_{\mu=k+1-TUB}^k v_{i,\mu(mod p)} \geq y_{i,k} \quad \forall i \in D, \forall k \in P$ (upper bound for shift length)

- $\sum_{\mu=k+1}^{k+R_{max}} v_{i,\mu(mod p)} \geq q_i - y_{i,k} \quad \forall i \in D, \forall k \in \{1..p - R_{max}\}$ (max rest between two consecutive shifts)

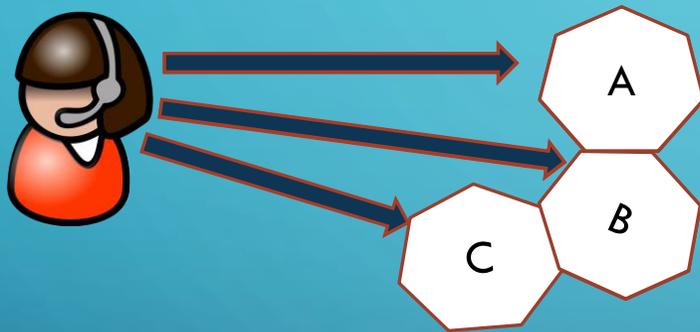
- $\sum_{\mu=k+1}^{k+R_{min}} v_{i,\mu(mod p)} \leq q_i - y_{i,k} \quad \forall i \in D, \forall k \in P$ (min rest between two consecutive shifts)

- **Constraints:**

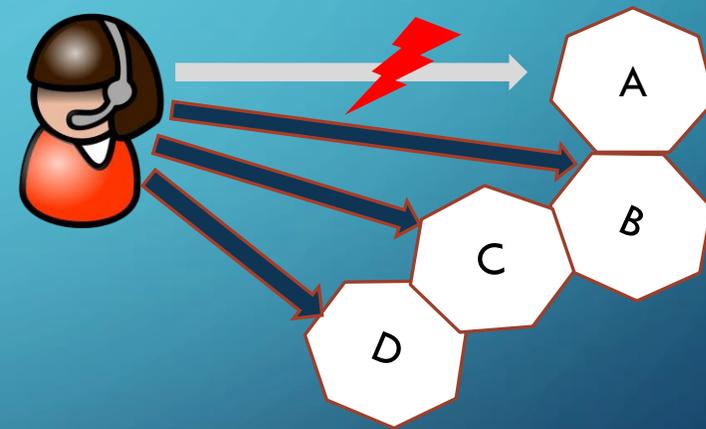
- $\sum_{i \in D} x_{i,j,k} = 1 \quad \forall j \in S, \forall k \in P: TL_{j,k} > 0$ (assign one dispatcher to area j during period k if j has positive task load)
- $\sum_{i \in D} x_{i,j,k} = 0 \quad \forall j \in S, \forall k \in P: TL_{j,k} = 0$ (no assignment for area j if there is no positive task load during period k)
- $v_{i,k} \leq q_i \quad \forall i \in D, \forall k \in P$ (if dispatcher i starts in some period then $q_i = 1$)

Extension of the original model

The issue for periods with no task load



Areas A, B and C have positive task load



Areas A has no task load and is substituted by D

- We introduce a new set:
 - V : set of 'virtual' geographic areas j' , such that $j' = j + 100$ for each element in D .
- We add new variables:
 - $Z_{i,j,k}$ (binary), equal to 1 if area switching is necessary due to capacity constraints.

- *New constraints:*

- $x_{i,j+100,k} = 0 \forall i \in D, \forall j \in S, \forall k \in P$ if $TL_{j,k} > 0$ (no virtual area is assigned whenever the task load is positive)
- $\sum_i x_{i,j,k} = 1 \forall j \in V, \forall k \in P$, if $TL_{j-100,k} = 0$ (assign the correspondent virtual area whenever the task load becomes null)
- $\sum_i (x_{i,j,k} + x_{i,j+100,k}) = 1 \forall j \in S, \forall k \in P$ (an area or its virtual correspondent is assigned to only one dispatcher during each period)

- *New constraints:*

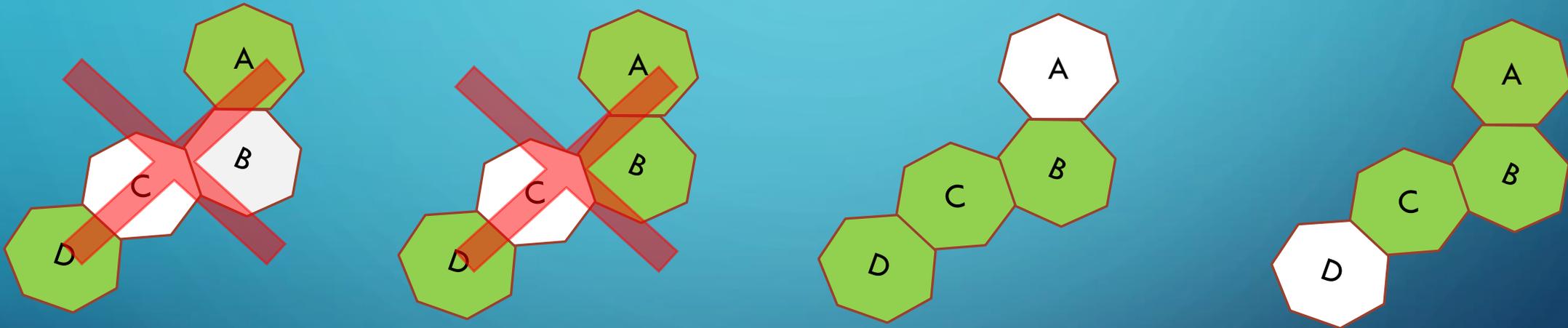
- $x_{i,j,(k+1) \bmod p} + y_{j,(k+1) \bmod p} - 1 \leq x_{i,j,(k+1) \bmod p} + z_{i,j,(k+1) \bmod p} \quad \forall i \in D, \forall j \in S, \forall k \in P$ if $TL_{j+(k+1) \bmod p} > 0$ (keep the same assigned area if a dispatcher is still working next period and the area still have a positive task load)
- $x_{i,j+100,k} + y_{j,(k+1) \bmod p} - 1 \leq x_{i,j,(k+1) \bmod p} + z_{i,j,(k+1) \bmod p} \quad \forall i \in D, \forall j \in S, \forall k \in P$, if $TL_{j,(k+1) \bmod p} > 0$ (keep the same assigned area (or its virtual) if, after being assigned to a virtual area, a dispatcher is still at work next period)
- $x_{i,j,k} + y_{j,(k+1) \bmod p} - 1 \leq x_{i,j+100,(k+1) \bmod p} + z_{i,j,(k+1) \bmod p} \quad \forall i \in D, \forall j \in S, \forall k \in P$, if $TL_{j,(k+1) \bmod p} = 0$ (if in next period a dispatcher is still at work and its assigned area has no task load then assign the correspondent virtual area)

A possible objective function is to minimize a linear combination of the total number of used dispatchers and the switches:

$$\text{Minimize } \sum_i \sum_j \sum_k \alpha * q_i + \beta * z_{i,j,k} \text{ with } \alpha \gg \beta$$

WHAT TO DO NEXT STEP?

- How to combine the geographical areas?



- Elaborate the data provided by BelOp to determine the workload thresholds

Expected output

shifts	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23
1																								
2																								
3																								
4																								
5																								
6																								
7																								
8																								

An example of one day schedule for eight dispatchers. This example was presented by Josefsson* et al.

*B. Josefsson, T. Polishchuk, V. Polishchuk, C. Schmidt, Scheduling Air Traffic Controllers at the Remote Tower Center, DASC (2017)

THANK YOU FOR LISTENING

shifts	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	
1																									
2																									
3																									
4																									
5																									
6																									
7																									
8																									

Questions?

